



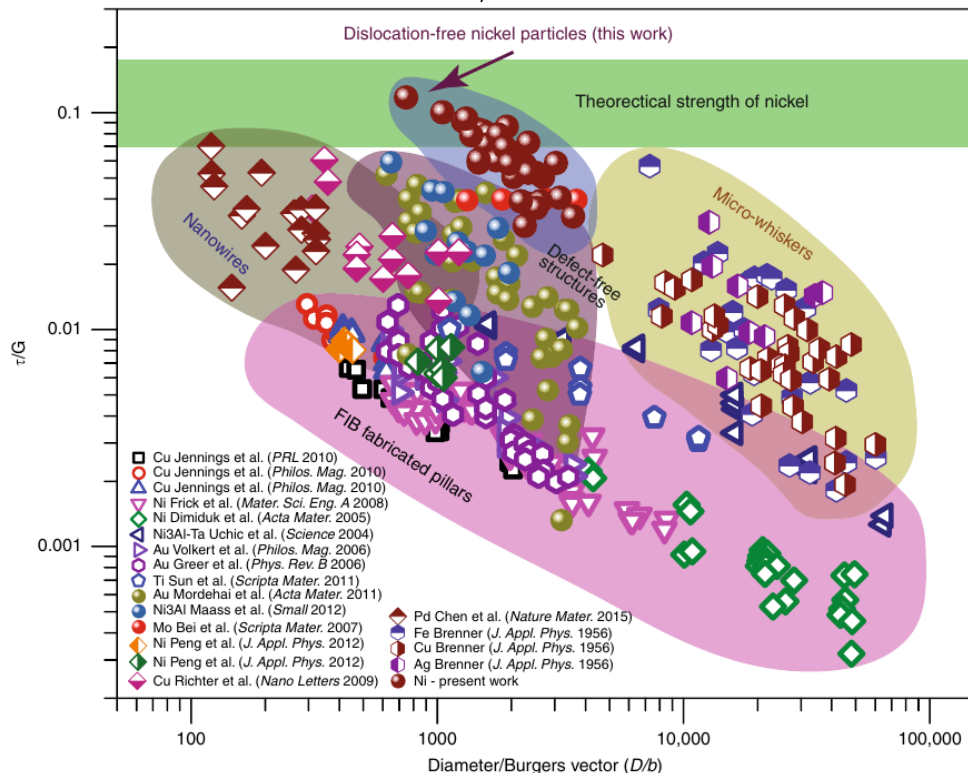
INSTITUT



# **Etude des propriétés mécaniques aux échelles nanométriques par dynamique moléculaire ab initio à température finie**

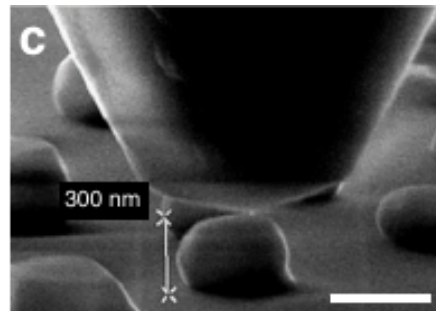
Laurent Pizzagalli  
CNRS - Institut Pprime  
Poitiers, France

Sharma et al., Nature Comm. 2018



→ Smaller is stronger  
 Very high strength values  
 Most studies concern 1D systems (nanopillars, whiskers)

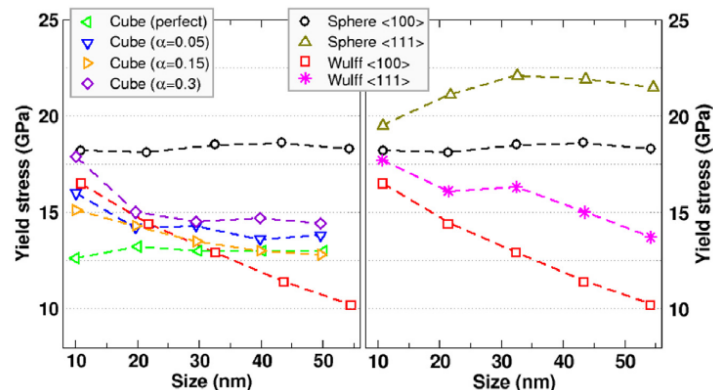
Sharma et al., Nature Comm. 2018



↓  
 Strength values even higher for nanoparticles  
 Reach theoretical strength values (Ni, Mo)

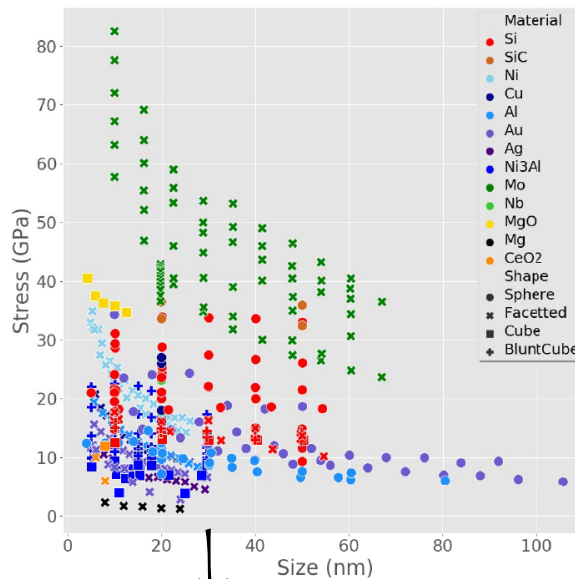
Does strength keep increasing when dimensions are further reduced ?  
 Experimentally challenging to explore smaller dimensions...

Kilymis et al., Acta Mat. 2018



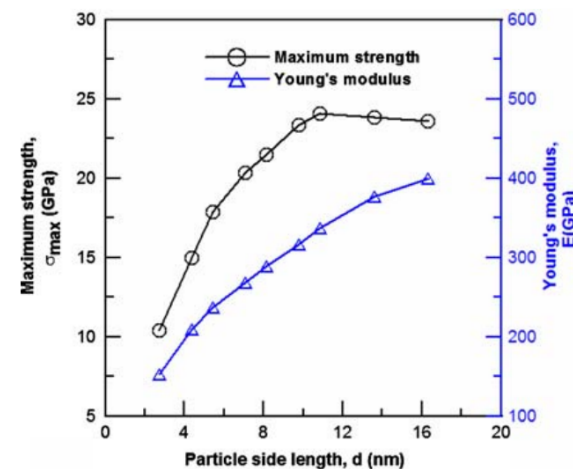
Shape dependency  
Plateau or increase

Amodeo et al., Comptes Rendus Physique 2021



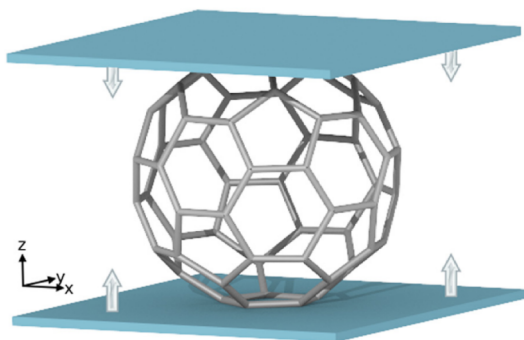
Shape and material dependency  
Mainly increases

Fang et al., J. Nanopart. Res. 2009



Decrease!

MD calculations of small ( $< 10\text{nm}$ ) systems are computationally cheap, but interatomic potentials are not necessarily reliable due to high strain, surfaces, electronic effects



Car-Parrinello MD DFT coupled with classical ionic force fields (why ?)

$$M_{\alpha} \ddot{\mathbf{R}}_{\alpha}(t) = - \frac{\partial}{\partial \mathbf{R}_{\alpha}(t)} E[\{\Psi(t)\}, \mathbf{R}(t)] + \mathbf{F}_{\alpha}[\mathbf{R}_{\alpha}(t), t]$$

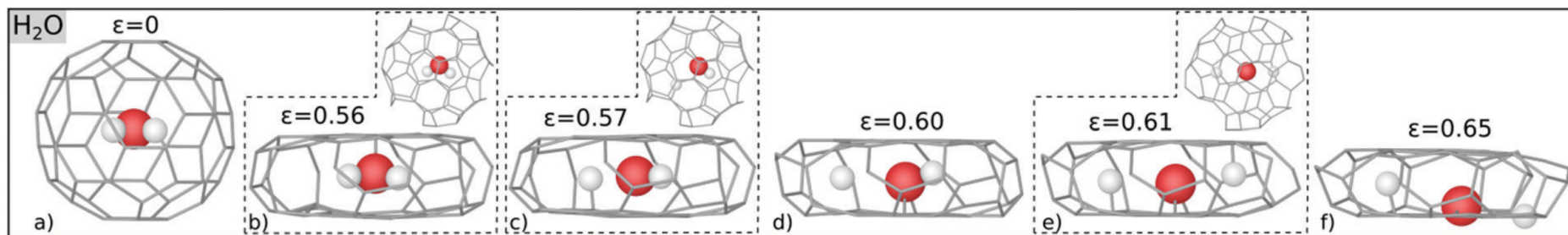
Pizzagalli, Phys. Rev. B 2020

Implemented in

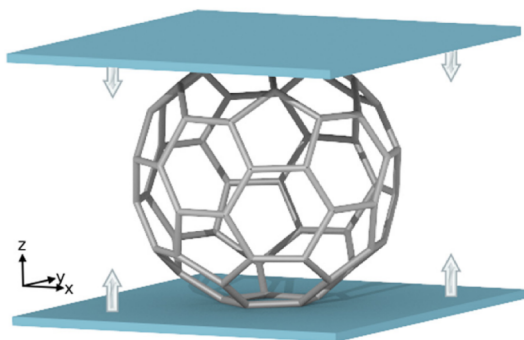


DFT accuracy  
Versatile and adaptable to polyatomic systems  
Much more costly than classical MD

Investigation of mechanical properties of endofullerenes:



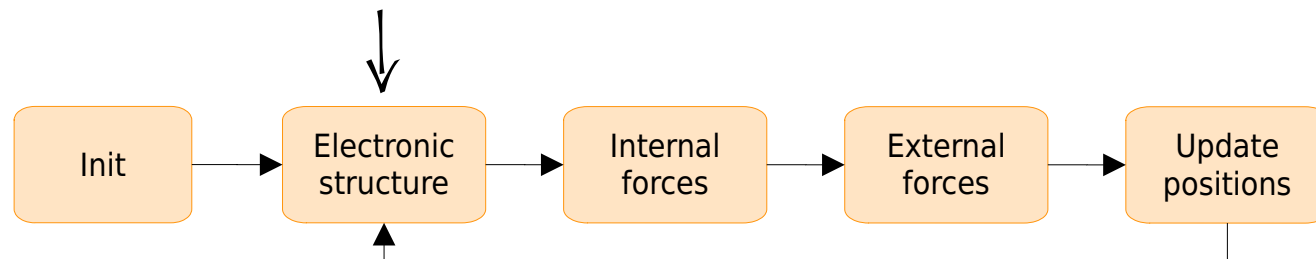
Pizzagalli, Phys. Chem. Chem. Phys. 2022



Implemented in

→ Gitlab/github  
Fortran

Computational effort essentially needed here

Example:  $\text{Si}_{147}\text{H}_{100}$  :

1 run using 288 cores

1 iteration (ions + electrons):  $\sim 2.5$  s

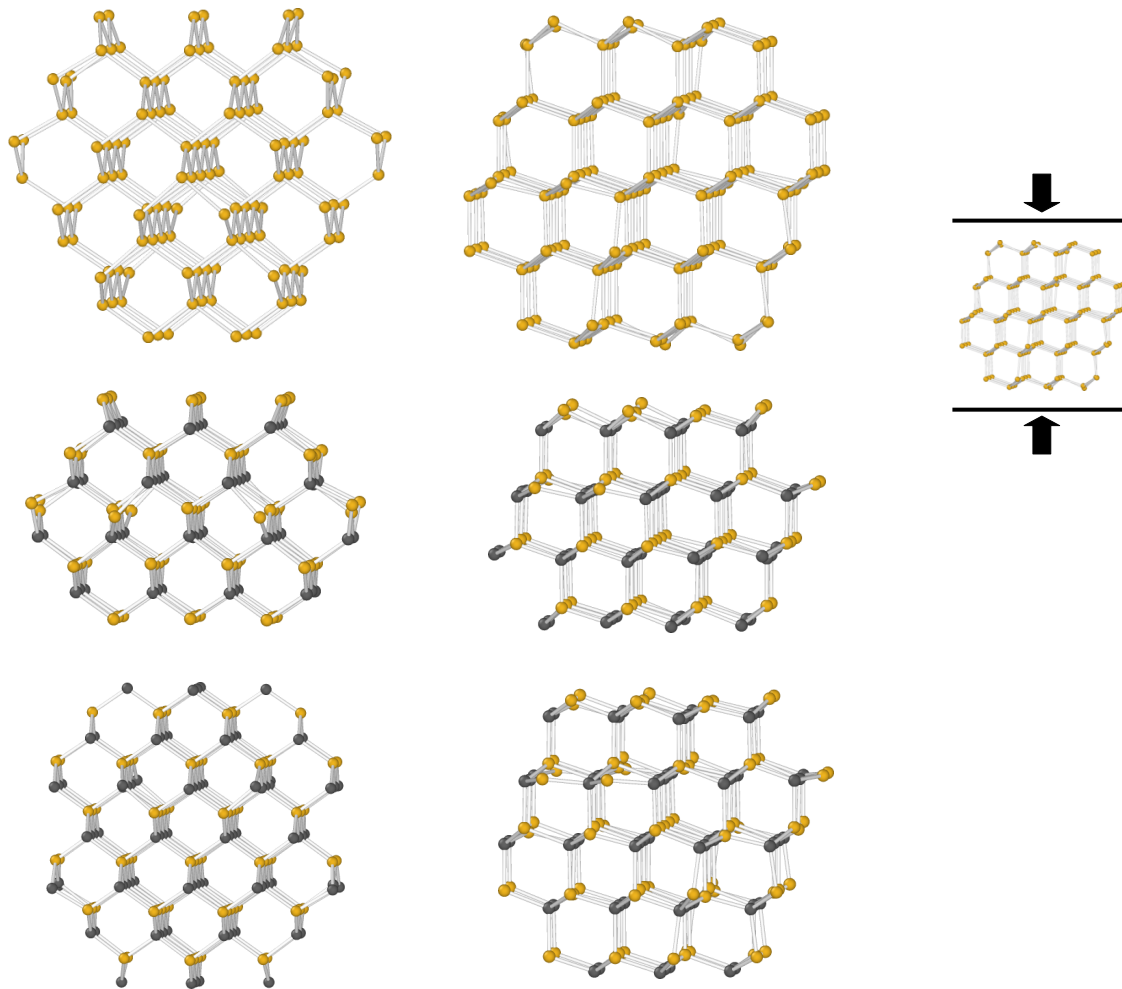
Efficient and fast MPI implementation

**BUT**

Strain rate is a critical factor in mechanical simulation (usually  $10^{11}$  faster than in 'normal' experiments)  
The timestep of the simulation is very small, lower than 1fs for Car-Parrinello MD



A large number of iterations is needed, about  $3 \times 10^5$  for a single run, i.e.  $\sim 200$ h for 288 cores (57600 h)  
Segmentation is possible and easy if the run termination is well controlled.

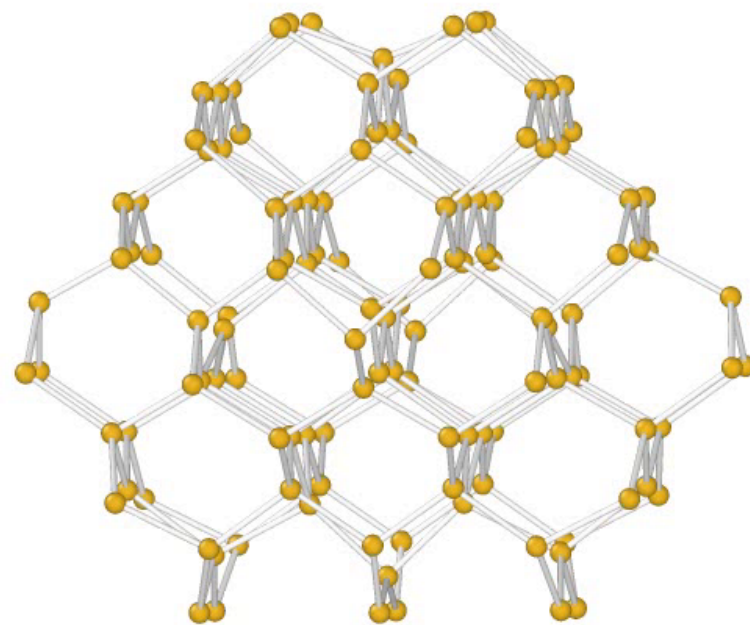
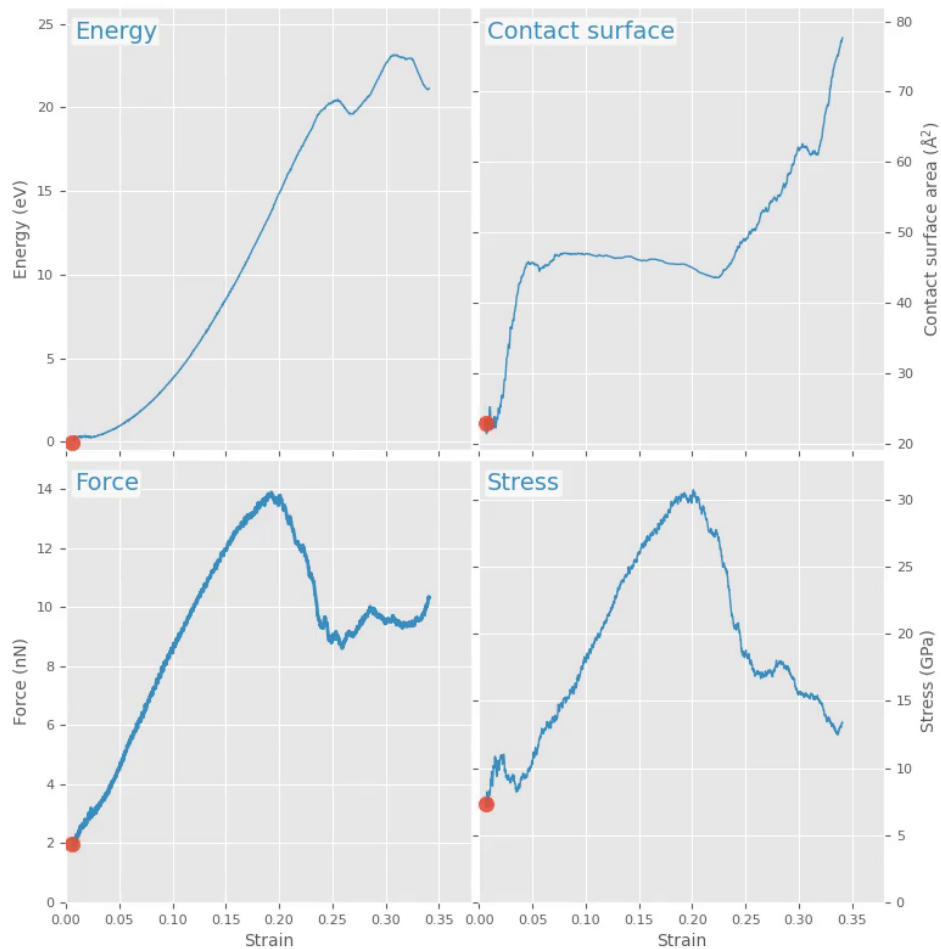


Si / SiC nanoparticles (quantum dots)  
<001> and <111> orientations  
Sizes: 1.1 - 1.8 nm

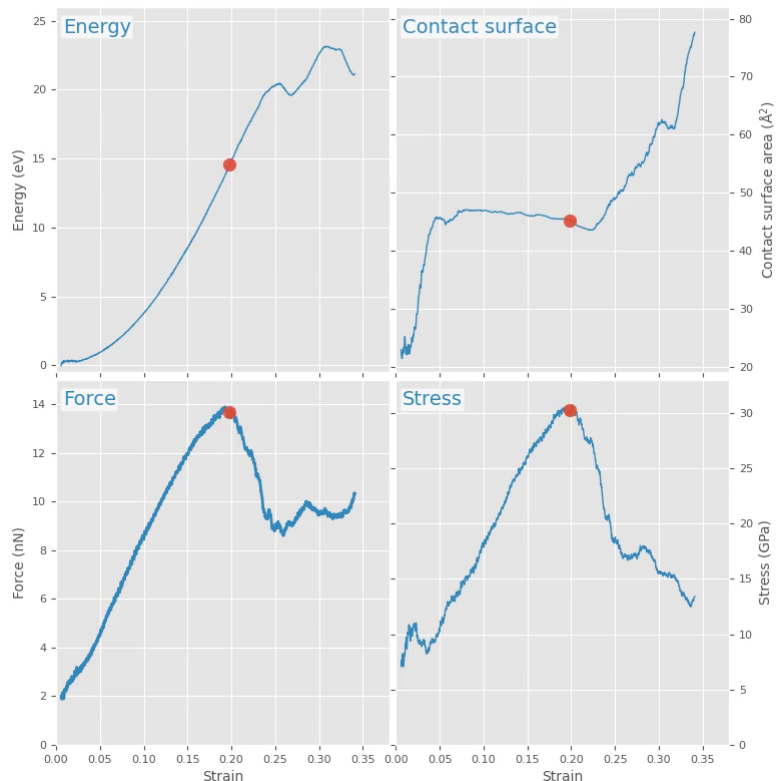
25 Ry cutoff  
 $\gamma$ -point sampling  
Ultrasoft pseudopotentials  
Isolated nanoparticles in a PBC supercell  
Ionic (300K) and electronic thermostats  
Surface atoms saturated by H  
MD Compression with two virtual flat punches

## Objectives:

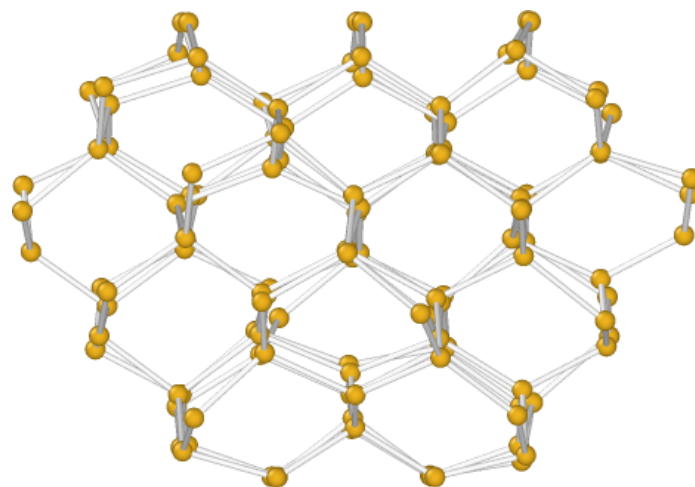
Strength and elastic limit determination  
Plasticity mechanisms

Si<sub>123</sub> <001> compression

Force / stress max. at  $\epsilon = 0.20$   
1<sup>st</sup> energy max. at  $\epsilon = 0.26$

$\epsilon = 0.20$ 

→ Force (13.8 nN) and stress (30 GPa) maxima  
 Energy inflexion point  
 Elastic deformation (?)

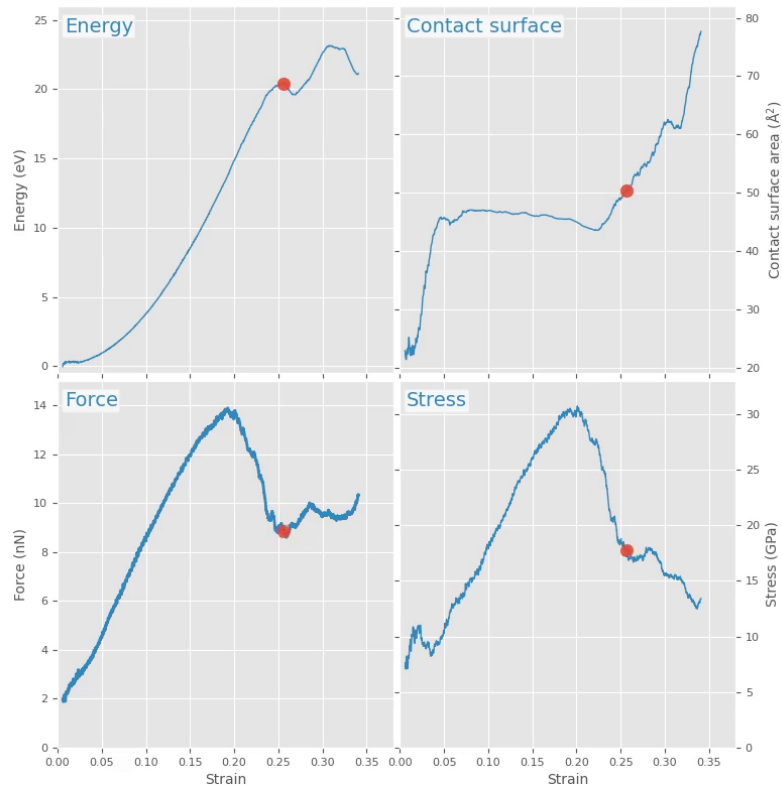


→ No visible “plastic” deformation

<001> softening: beginning of diamond →  $\beta$ -tin transition (shear softening) (Needs & Mujica Phys. Rev. B 1995)  
 No  $\beta$ -tin because deconfinement effect in nanoparticles (Chrobak et al, Nature Nanotechnology 2011)  
 Stress maximum does not imply plasticity !!!

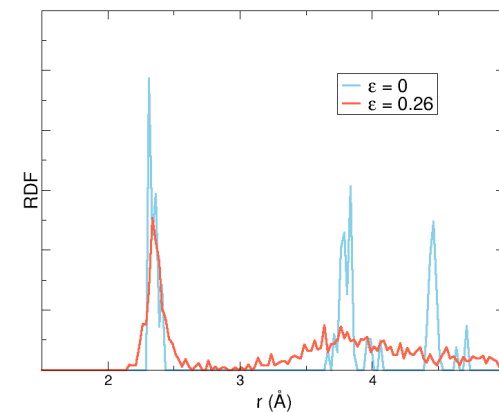
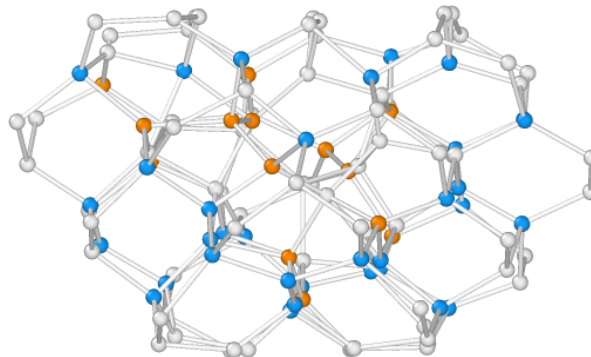


# Si nanoparticle compression: amorphization

 $\epsilon = 0.26$ 


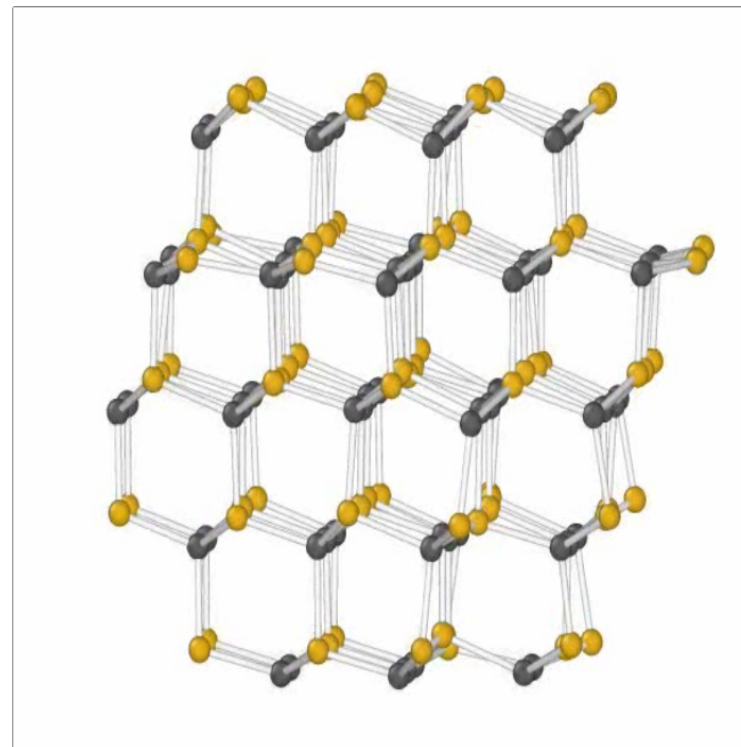
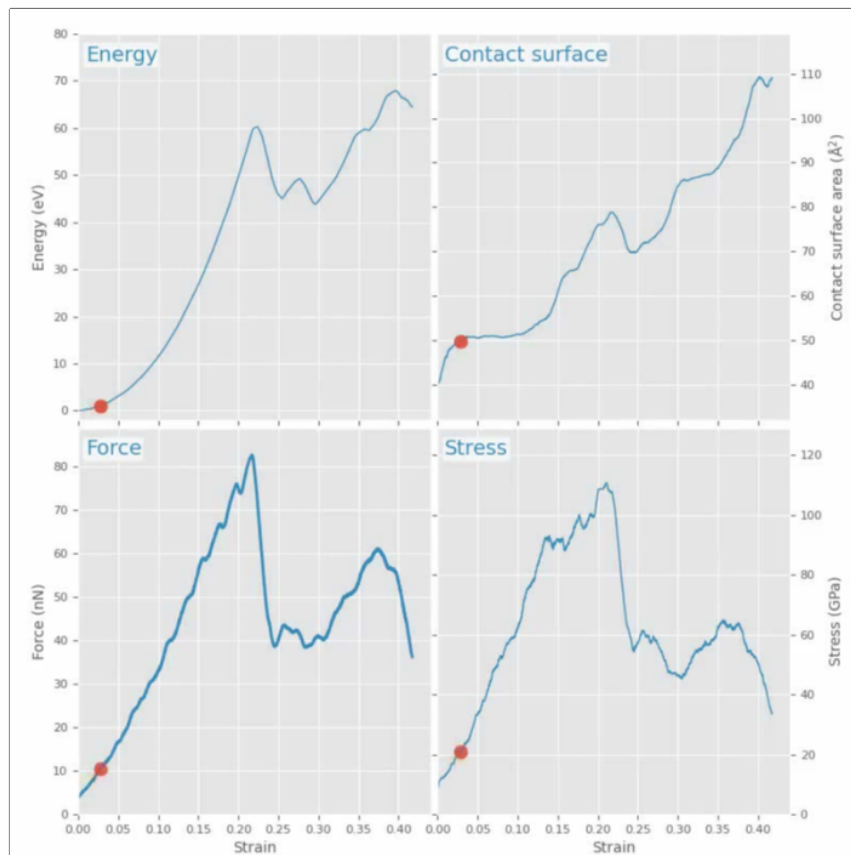
→ Energy maximum (20 eV)  
 Force minimum  
 Plastic deformation

Polyedral template matching analysis  
(Mahler Larsen et al, MSMSE 2016)



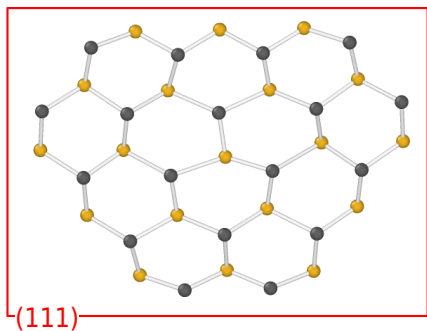
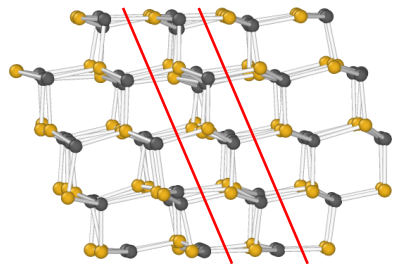
Elastic - plastic transition by amorphization  
 Low dimensions improve a-Si phase stability (Tolbert et al, PRL 1996)

SiC<sub>141</sub> <111> compression



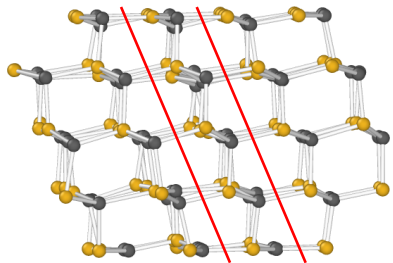
Force / stress / energy max. at  $\epsilon = 0.21$   
Other "events" at  $\epsilon = 0.26 / 0.37$

$\epsilon = 0.223$     $\sigma = 100$  GPa

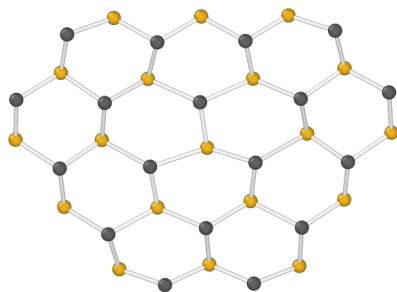
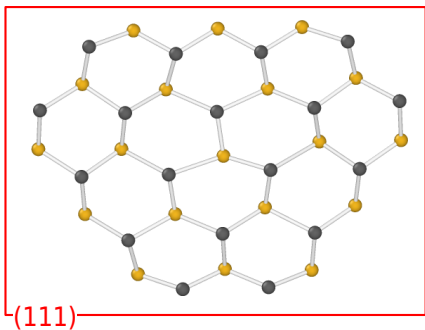


# SiC nanoparticle compression: dislocation formation?

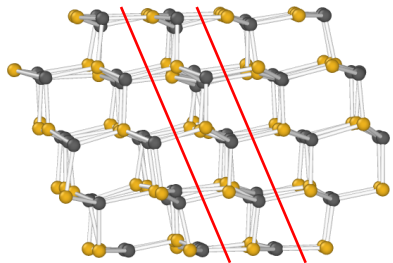
$$\epsilon = 0.223 \quad \sigma = 100 \text{ GPa}$$



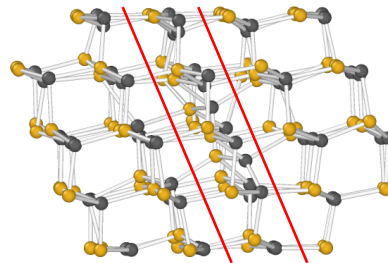
Concerted motion  
of 4 atoms



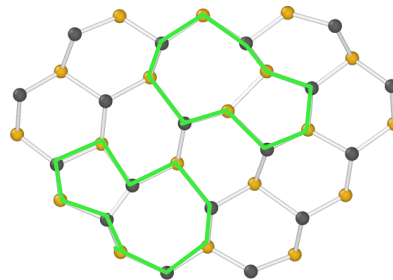
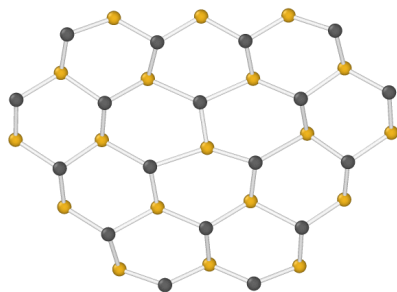
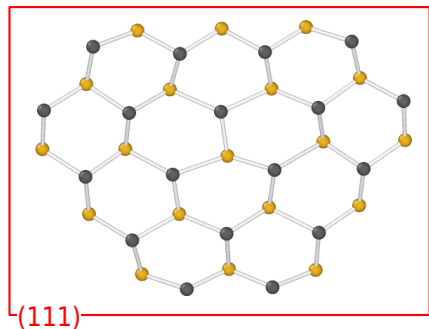
$\epsilon = 0.223$     $\sigma = 100$  GPa



$\epsilon = 0.225$

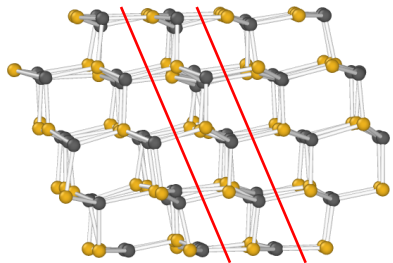


Concerted motion  
of 4 atoms

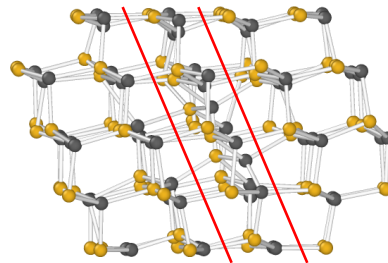


Point defects dipole  
BUT equivalent to the formation  
of a dislocation loop in (111) plane  
with  $\mathbf{b} // \langle 110 \rangle$  ( $|\mathbf{b}| < \frac{1}{2} |110|$ )

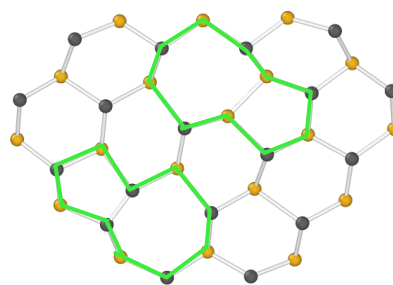
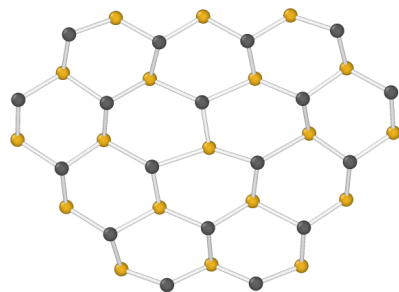
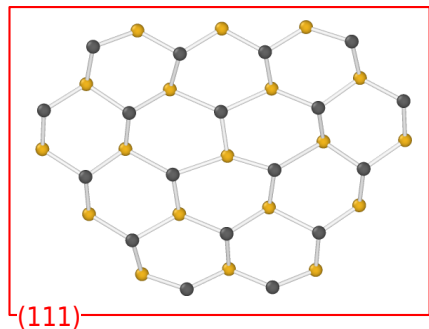
$\epsilon = 0.223$   $\sigma = 100$  GPa



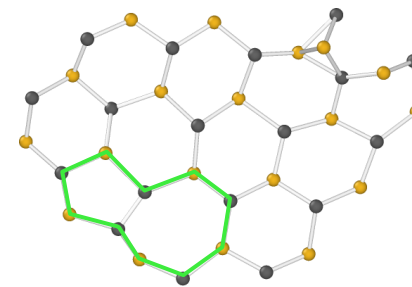
$\epsilon = 0.225$



Concerted motion of 4 atoms

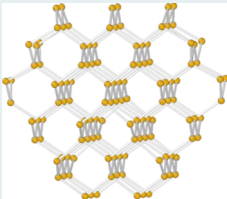
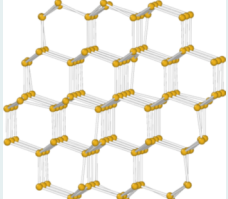
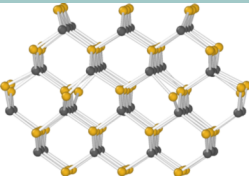
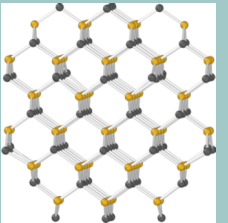
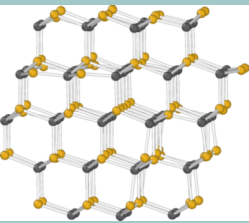
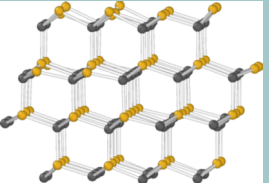


$\epsilon = 0.242$   $\sigma = 57$  GPa



Point defects dipole  
BUT equivalent to the formation of a dislocation loop in (111) plane with  $\mathbf{b} // \langle 110 \rangle$  ( $|\mathbf{b}| = \frac{1}{2}|\langle 110 \rangle|$ )

Suggests homogeneous nucleation of dislocation is possible in nanoparticles of 1-2 nm  
Partial Burgers vector, in agreement with previous studies (Gutkin et al Acta Mat. 2008, Miller et al. JMPS 2008)  
Loop expansion is prevented by large stress decrease

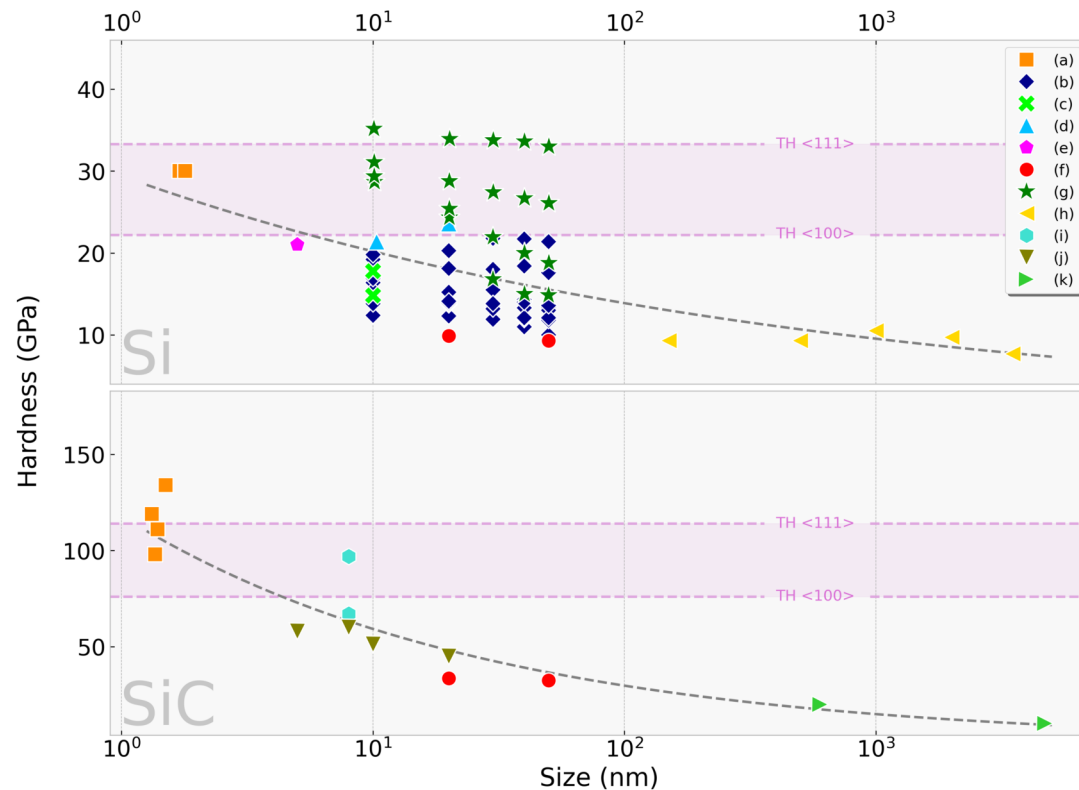
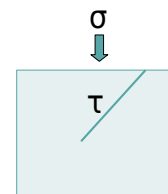
					
Si - 123 - <001>	Si - 148 - <111>	SiC - 127 - <001>	SiC - 172 - <001>	SiC - 147 - <111>	SiC - 122 - <111>
$\epsilon = 0.26$ $\sigma = 30$ GPa	$\epsilon = 0.195$ $\sigma = 30$ GPa	$\epsilon = 0.28$ $\sigma = 98$ GPa	$\epsilon = 0.30$ $\sigma = 134$ GPa	$\epsilon = 0.21$ $\sigma = 111$ GPa	$\epsilon = 0.25$ $\sigma = 119$ GPa
→ Softening → Amorphization	→ Amorphization	→ Amorphization	→ NP rotation → Amorphization	→ Dislocation-like → Surface crack → Amorphization	→ Dislocation-like → Amorphization

Amorphization the most common mechanism (might be related to the high deformation speed)

Dislocation-like formation possible in small NP (but limited expansion due to stress release / low temperature)

“Grain” or surface-related mechanisms can be activated (nanoparticle rotation, surface crack)

# Ultimate compressive stress



$\tau(\text{Si}) = 9.1 \text{ GPa}$   
 $\tau(\text{SiC}) = 31 \text{ GPa}$

Schmid law:  $H \equiv \sigma = \tau/m$

$m(\langle 111 \rangle) = 0.272$   
 $m(\langle 001 \rangle) = 0.408$

$H(\text{Si}) = 22.2 \text{ GPa } \langle 001 \rangle$   
 $= 33.3 \text{ GPa } \langle 111 \rangle$   
 $H(\text{SiC}) = 76 \text{ GPa } \langle 001 \rangle$   
 $= 114 \text{ GPa } \langle 111 \rangle$

- (a) This work
- (b) Kilymis et al, Acta Mat. 2018
- (c) Hale et al, Comp. Mat. Sci. 2011
- (d) Chrobak et al, Nat. Nanotech. 2011
- (e) Valentini et al, PRL 2007
- (f) Kilymis et al, Acta Mat. 2019
- (g) Hong et al, Acta Mat. 2018
- (h) Chen et al, Nat. Com. 2020
- (i) He et al, J. Nano. Res. 2016
- (j) Kayang et al, Appl. Phys. A 2021
- (k) Shin et al, JACS 2012

Stress increases when size decreases, up to the tiniest nanoparticles/quantum dots  
 Theoretical strength can be reached (exceeded?) in these systems, or Schmid law cannot be used

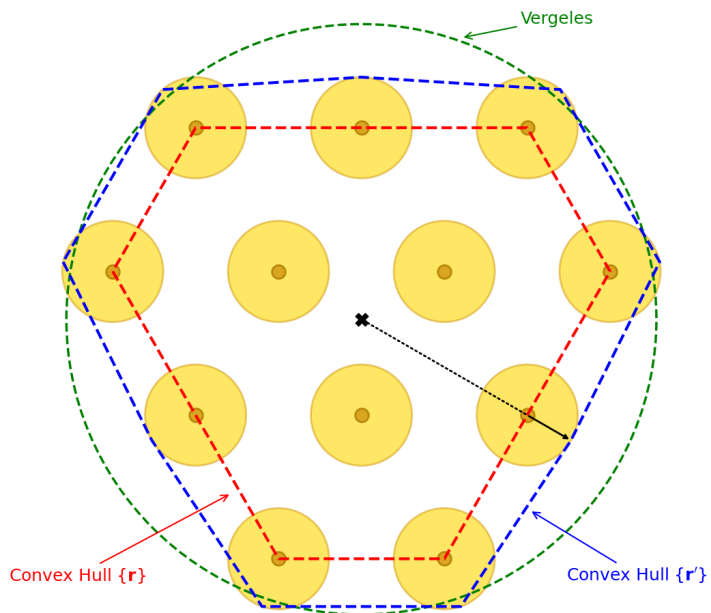


DFT molecular dynamics compression of Si/SiC nanoparticles

- Several plasticity mechanisms (amorphization, dislocation, surface-related, grains) revealed
- The homogeneous nucleation of dislocation is possible in very small systems
- High yield stress and strain values, theoretical bulk strength is reached and even exceeded
- Suggests that strength value increases up to the theoretical value (no plateau and no decrease): at least for covalent systems like Si/SiC

**Todo next:**

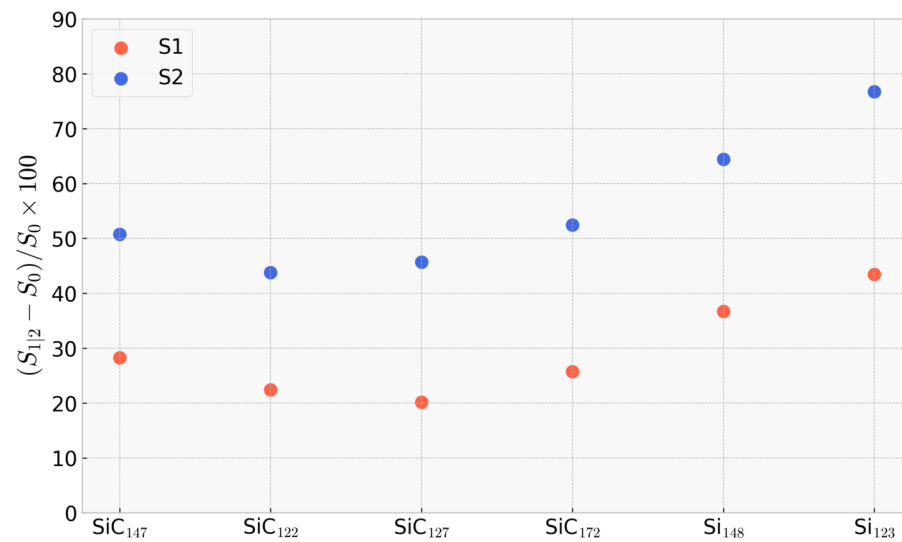
- Development of a similar approach using Born-Oppenheimer dynamics and application to metallic nanoparticles
- Time increase for one ionic iteration (but a slightly larger timestep can be used)
- Need for more computational resources....



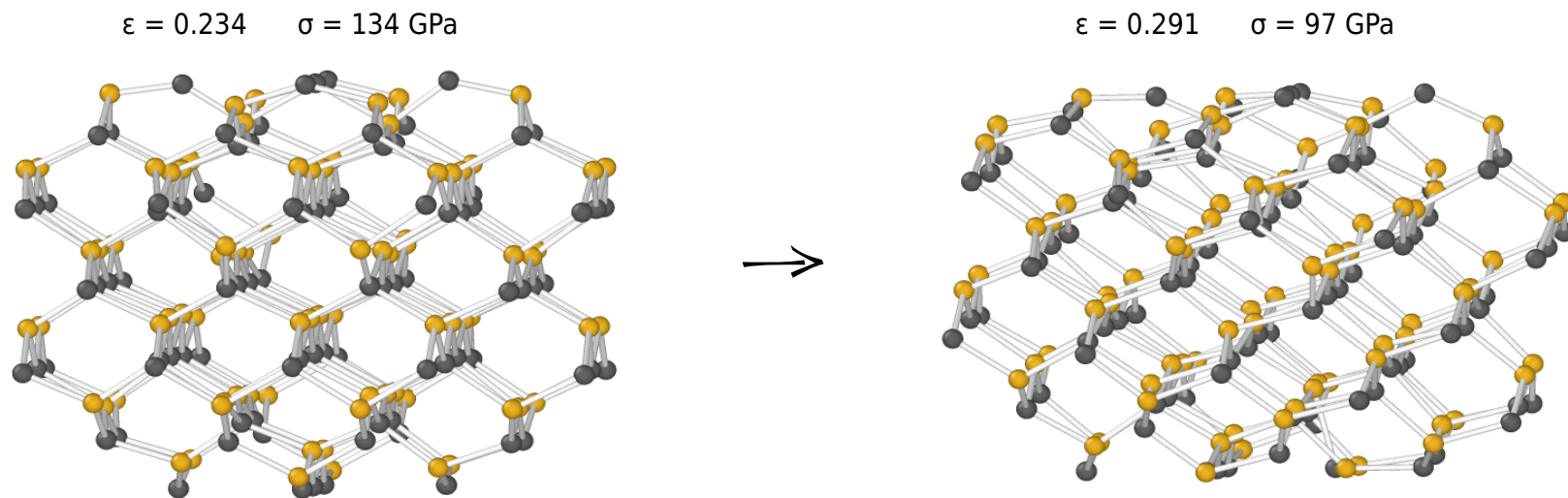
S1 appears as a reasonable “measure” of the contact surface area

What is the best approximation of the contact surface?

- Vergeles : overestimation, not suited for non-circular contact
- Convex hull ( $S_0$ ) : lower limit
- Convex hull + corrections:  $S_1 = S_0 + w(n)\Sigma s_c$
- “Augmented” convex hull ( $S_2$ ) : upper limit

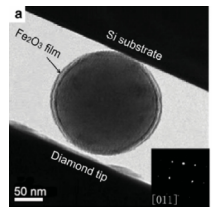


SiC<sub>172</sub> <001> compression

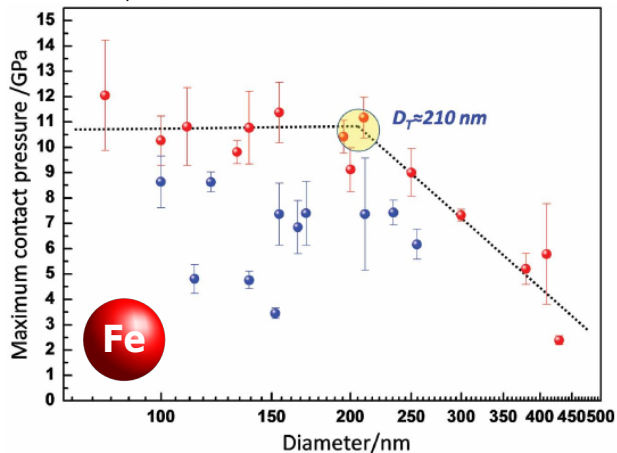


Max. stress corresponds to the rotation of the NP surface area: 'grain'-like mechanism  
Due essentially to a contact surface increase  
No energy and force maxima: suggests that the deformation remains elastic

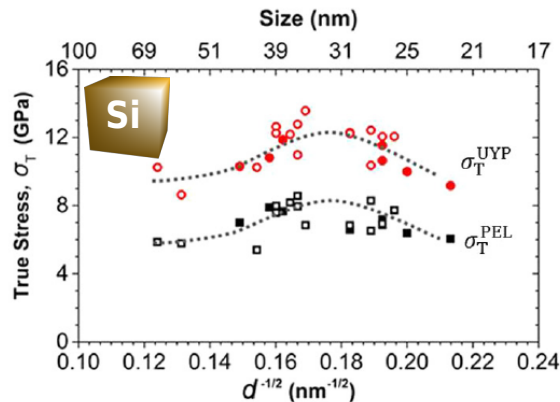
# Limits at ultra small scales?



Han et al., Adv. Func. Mat. 2015

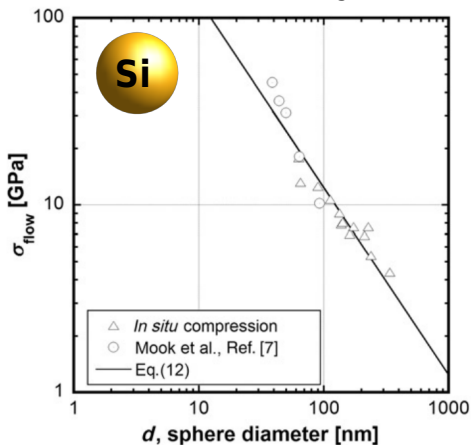


Wagner et al., Acta Mat. 2015



→ Plateau at low dimensions?

Beaber et al., Philos. Mag. 2011



→ No plateau?

Materials dependency?  
 Shape (material) dependency?  
 Extrinsic effects (coatings)?  
 Hardness/strength definition...

Many unanswered questions!!!  
 But experimentally challenging to explore smaller dimensions